Laser-Doppler Blood Perfusion Flowmetry for studying Post-Occlusion Reactive Hyperaemia and Drug Administration by Iontophoresis

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Contents:

- Principles of Laser-Doppler Blood Perfusion Monitoring
 - Model for Post-Occlusion Reactive Hyperaemia (PORH) to study Peripheral Arterial Occlusive Disease (PAOD)
 - 3. Model for Drug Administration using Iontophoresis

Publications: see website: www.demul.net/frits, scroll to "Laser Doppler".

LDV: Principles

Principle of Laser-Doppler Blood Flow Perfusion Monitoring in Tissue

- A laser beam with pencil shape will be scattered
- by structures (particles, cells, vessels, ...) in tissue.
- If these structures have a **velocity**
- the scattered light will get a slight **Doppler frequency shift**.
- This shift can be measured by **mixing** the emerging light
- with the original **incident** light.
- The shift is **proportional** to the averaged (*) particle **velocity**
- and the **amount** of scattering particles involved.
- (*) "averaged": over directions and magnitudes of particle velocities

LDV: Principles

Principle of laser Doppler:



v : particle velocity

 k_0 and k_s : incoming and scattered wavevectors $k = 2\pi/\lambda$; λ = wavelength

 $\omega_D = 2\pi f_D$: Doppler frequency

$$\omega_D = \left(\vec{k}_s - \vec{k}_o\right) \bullet \vec{v}$$

$$f_D = \frac{kv}{\pi} \sin \frac{1}{2} \theta \cos \alpha$$

Normally in tissue: θ is small : $\langle \theta \rangle \langle \approx 10^{\circ}$ \Rightarrow approx.: $\delta k \perp k_0, k_s$: only *v*-component $\perp k_0$ measured

LDV: Types of Instruments (1)

(A) Differential (Dual-beam) Laser Doppler Velocimetry

Interference fringe pattern



LDV: Types of Instruments (2)

(A) Differential (Dual-beam) Laser Doppler Velocimetry



1. Original frequency $\omega ~ [\approx 10^{14} \text{ Hz}]$

2. Doppler-shifted frequency $\omega + \omega_D \quad [\approx 10^{14} \text{ Hz}]$

3. Doppler frequency ω_D [< \approx 20 kHz]

4. Doppler intensity signal : \sim (freq.sign)²

LDV: Types of Instruments (3)

(B) Laser Doppler Perfusion Velocimetry



- (multiple) scattering in random directions

LDPV: Spectra (1)

(B) Laser Doppler Perfusion Velocimetry



Heterodyne peak: due to large amount of non-Doppler shifted scattered photons.

LDPV: Spectra (2)

(B) Laser Doppler Perfusion Velocimetry



Power spectrum depends on:

- concentration *C*

- velocity V

Moments of Power spectrum :

$$M_n = \int_0^\infty \omega^n . S(\omega) d\omega$$
$$(n = 0, 1, 2, ...)$$

Moments:

 M_0 : ~ concentration of moving scatterers M_1 : ~ flux of moving scatterers M_1/M_0 : ~ velocity

LDPV

(B) Laser Doppler Perfusion Velocimetry



LDPV: Instruments

(B) Laser Doppler Perfusion Velocimetry: Instrument design





- (a) Glass fibers for light transport
 - Disadvantages:
 - motional artefacts
 - sensitive for local variations

(b) Direct-contact velocimetry: Laser and detector in one probe



- no motional artefacts
- local averaging

LDPV: Signals

(B) Laser Doppler Perfusion Velocimetry

LD spectra of finger tip upon occlusion of upper arm

> See software package LASDOPP



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LDPV: Skin Tissue



(B) Laser Doppler Perfusion Velocimetry

Schematic cross section of Skin tissue

Needed: Data about perfusion of different layers at different depths

LDPV: Instruments

(B) Laser Doppler Perfusion Velocimetry: Instrument designDepth sensitive sensor

- use detectors at different distances from the light source (see fig.)
- use different colors (red light probes deeper than green)







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A model for PORH (Post-Occlusion Reactive Hyperemia), as measured with Laser-Doppler Perfusion Monitoring

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Fernando Morales Ruiz

Andries J. Smit

Reindert Graaff

Jan Aarnoudse

Microcirculation:

blood flow through **microvasculature** (< 1 mm diameter)

Regulation of microcirculation:

- controlled by **musculature** of the arterioles
- based on ambient temperature and/or concentration of metabolism-related substances (O₂, CO₂, NO...)
- > operating through vasodilatation

Peripheral Arterial Occlusive Disease (PAOD):

- stenoses in proximal arteries.
- decrease of available pressure level in arterioles
- vasodilatation impaired or delayed

- > Post-Occlusive Reactive Hyperemia (PORH)-test:
 - > to assess microvascular functioning
- Procedure of PORH:
 - arterial occlusion upstream in artery to extremity
 - before, during and after **arterial occlusion:**
 - local blood perfusion measured at **distal extremity** as function of time

• PORH-test procedure



Measured data (typical)

(all measurements by F. Morales)





MF = maximum, HF = half decrease time between maximum and resting flux, t_{RF} = time of cross point with **RF**.

PAOD vs. Healthy:

- Longer time scales
- Rise time and Decrease time tend to become equal
- Decreased overshoot maximum

Similar behaviour for Diabetes patients

•Building blocks for the flow model:

I: Flow
$$[m^3/s]$$

V: Pressure [Pa = $N/m^2 = J/m^3$]

Electrical analogon *I* : Current [C/s = A] *V* : Voltage [V = J/C]



- μ = viscosity [Ns/m²]
- l = tube length [m]
- R_0 = tube radius [m]
- E = Young's elasticity modulus [N/m²]
- *h* = tube wall thickness [m]

$$\rho$$
 = density [kg/m³]

- Model:
- Two sub-models: "arterial" and "capillary"
- "Arterial" part: flow resistance + compliance
- "Capillary" part: time-dependent flow resistance



- I is the flow measured by LDF
- R_{leak} accounts for possible flow leakage passing capillary system

• Model with details:

• Two sub-models: "arterial" and "capillary"



R's are resistances (narrow tubes) *C*'s are compliances (storage vessels)

• Model with details:

• Two sub-models: "arterial" and "capillary"



Small times: C_2 small impedance $\rightarrow R_{cap} \approx R_2 \rightarrow \text{flow } I$ large Large times: C_2 large impedance $\rightarrow R_{cap} \approx R_2 + R_3 \rightarrow \text{flow } I$ small



upon cuff release after occlusion:

(Electrical: sudden voltage V_0)

$$I_2 = a_0 \left[1 - a_1 \exp(-p_1 t) - (1 - a_1) \exp(-p_2 t) \right]$$

with
$$a_0, a_1, p_1, p_2 = f(R_1, R_2, R_3, R_4, C_1, C_2)$$

NB. Two exponentials, both decreasing in time.

$$I_2 = a_0 \left[1 - a_1 \exp(-p_1 t) - (1 - a_1) \exp(-p_2 t) \right]$$

- at time t = 0: $I_2 = a_0 [1 - a_1 - (1 - a_1)] = 0$
- at time $t \to \infty$: $I_2 \to a_0 \ [1 - 0 - 0] = a_0$

With $p_1 = 1/\tau_1$ and $p_2 = 1/\tau_2$:

- τ_1 and τ_2 : characteristic times
- If $\tau_1 < \tau_2$: see figure \rightarrow



Approximation:

- "Arterial" much faster than "capillary" →
- Two separate submodels: "arterial" and "capillary"
- $R_4 \rightarrow \infty$



$$V_1 = V_0 \left(1 - e^{-t/\tau_1} \right) \qquad \tau_1 = R_1 C_1$$

$$I_{2} = \frac{V_{1}}{R_{2} + R_{3}} \left(1 + \frac{R_{3}}{R_{2}} e^{-t/\tau_{2}} \right)$$

$$\tau_2 = C_2 \frac{R_2 R_3}{R_2 + R_3}$$







• approximation:





$$I_2 = \frac{V_1}{R_2 + R_3} \left(1 + \frac{R_3}{R_2} e^{-t/\tau_2} \right)$$

Even better approx.:

$$I_{2} = \frac{V_{1}}{R_{1} + R_{2} + R_{3}} \left(1 + \frac{R_{3}}{R_{2}} e^{-t/\tau_{2}} \right)$$



Question: when can we use the approximation ?





Examples of fitting: program LASDOP:

• Model fitting : two examples:

Healthy person (upper) and PAOD-patient (lower; down shifted -20)



Lower figure metades sine-approx. or vasomotion

- Model fits:
- Model parameters for recordings of a typical healthy person and a typical PAOD-patient

Person	Model	$\tau_1(\text{sec})$	$\tau_2(\text{sec})$			arterial
Healthy	Exact Approx	4.6 4.7	81.2 81.2	I_2	total	capillary
PAOD	Exact Approx	80 314	86 114		- τ	4:000

Healthy persons: exact model and approximation coincide; and render similar parameter values: indication for: "arterial part" faster than "capillary part".

PAOD-persons: models have very different parameters; Both "arterial part" and "capillary part" are slow.



"Area": Ratio of areas between measured data and extrapolated resting flux RF, for Reactive Hyperemia period (PORH) vs. Occlusion period (Oc).

Indicates compensation of oxygen debt from Occlusion period in the PORH period.

• Model fits: Signal strengths

Ratio of maximum flux vs. resting flux: no significant differences between healthy, Diabetes M. and PAOD:

 3.1 ± 0.6 for PAOD-group (N=7) 5.8 ± 4.8 for Diabetes M.-group (N=9) 3.2 ± 2.7 for healthy group (N=8)

Overall signal strength: No significant differences

- Conclusions from model fitting:
- 1. Exact model fits all measurements
- 2. Approximate model fits healthy group only
- 3. Response time:
 - a. "Arterial part": Healthy group faster than Diabetes-M.-group and much faster than PAOD-group
 - b. "Capillary part": \approx similar response time for all
- 4. Signal strengths (resting flux and maximum flux): no significant differences between groups
- 5. Area ratio between (PORH-RF) and (Occl.-RF) signals
 < 1 (aver. 0.6; healthy pers.) and >1 (aver. 1.5; POAD
 (Indicates compensation of oxygen debt from occlusion period)

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A Diffusion Model for Drug Administration by Iontophoresis, as measured with Laser-Doppler Perfusion Flowmetry

> Frits F.M. de Mul, Judith Blaauw, Jan Aarnoudse

- Goal of the project:
 - Model to characterise Iontophoresis,
 - As measured with Laser-Doppler blood perfusion flowmetry in capillaries in extremities,
 - Application: preeclampsia,
 - Characteristics:
 - 1-dim. Diffusion of concentration
 - Decay term (removal)
 - Saturation with subsequent iontophoretic shots.

Typical iontophoresis recording



("occlusion" performed to measure biological zero level)

Laser-Doppler probe for Iontophoresis



Typical dimensions: <u>probe</u>: <u>diameter</u> 10-20 mm, <u>height</u> 5-10 mm; <u>fiber separation</u> 250 μm.

The diffusion can be considered as mono-dimensional (in depth direction).

- The model:
- 1. 1-Dimensional diffusion
- 2. Decay (removal)
- 3. Saturation with subsequent shots.

- The model:
- 1. 1-Dimensional diffusion
- 2. Decay
- 3. Saturation by subsequent shots.

1. 1-Dimensional diffusion

$$\frac{\partial c}{\partial t} = D \frac{\partial^2 c}{\partial z^2}$$

$$t = \text{time [s]}$$

 $z = \text{depth [m]}$
 $c = \text{concentration [kg/m3]}$
 $D = \text{diffusion coefficient [m2/s]}$

$$c=f(z\,,\,t)$$

Start (boundary condition) for c(z,t): concentration "pulse" at z=0 and t=0.

$$c(0,0) = c_0$$
, with $\int_0^\infty c(z,t)dz = Q$ for all *t*, including $t = 0$

 $Q \sim \text{total amount of administered molecules}$



 $\frac{\partial c}{\partial t} = \text{increase of } c \text{ in time}$ $\frac{\partial c}{\partial z} = \text{increase of } c \text{ in space (slope)}$ $\frac{\partial^2 c}{\partial z^2} = \frac{\partial}{\partial z} (\frac{\partial c}{\partial z}) = \text{change in slope}$

Example: c = children on a slide:

No change in slope \rightarrow No increase of # children in time

Change in slope present. \rightarrow Increase of # children in time

D is proportionality constant

The model

- 1. 1-Dimensional diffusion
- 2. Decay
- 3. Saturation by subsequent shots.

1-Dimensional diffusion : solution

$$\frac{\partial c}{\partial t} = D \frac{\partial^2 c}{\partial z^2} \implies c(z,t) = \frac{Q}{\sqrt{\pi Dt}} \exp\{-\frac{z^2}{4Dt}\}$$



Q = amount of injected molecules

Parameter in fig.: depth z Constants in fig.: D = 0.001Q = 1

Drawback: decrease by diffusion only is too slow But : decrease by leakage (sideways) will also be present

The model:

- 1. 1-Dimensional diffusion
- 2. Decay
- 3. Saturation by subsequent shots.

2. Experiments show: Decrease in time too slow: Add decay term: $-\lambda c$

$$\frac{\partial c}{\partial t} = D \frac{\partial^2 c}{\partial z^2} - \lambda c \implies c(z,t) = \frac{Q}{\sqrt{\pi Dt}} \exp\{-\frac{z^2}{4Dt} - \lambda t\}$$

if
$$D = 0$$
: $c(t) = c(0).\exp(-\lambda t)$

Without decay



40

50

time

60



47

0.1

0.2

.....0.4

- - • 0.7

90

100

80

70

The model:

- 1. 1-Dimensional diffusion
- 2. Decay
- 3. Saturation by subsequent shots.

Assume:

excess (*) flow $\Delta F(t)$ ~ concentration (*) = above resting flux level.

$$c(z,t) = \frac{Q}{\sqrt{\pi Dt}} \exp\{-\frac{z^2}{4Dt} - \lambda t\} \implies \Delta F(t) = \frac{Q_0}{\sqrt{\pi Dt}} \exp\left(-\frac{z^2}{4Dt} - \lambda t\right)$$

Assume: N shots with interval Δt

$$\Delta F(t) = \sum_{n=1}^{N} \exp\left[-(n-1)s\right] \frac{Q_0}{\sqrt{\pi Dt_n}} \exp\left(-\frac{z^2}{4Dt_n} - \lambda t_n\right)$$

$$t_n = t - (n-1)\Delta t$$

s = shot saturation constant;

if *s* = 0: all shots contribute equally (exp=1) if *s* >>1: only first shot contributes (n=1 only)



The model:

- 1. 1-Dimensional diffusion
- 2. Decay
- 3. Saturation by subsequent shots.

Final model:

$$\Delta F(t) = \sum_{n=1}^{N} \exp\left[-(n-1)s\right] \frac{Q_0}{\sqrt{\pi Dt_n}} \exp\left(-\frac{z^2}{4Dt_n} - \lambda t_n\right)$$
$$t_n = t - (n-1)\Delta t$$

Notation in program:

$$\Delta F = \sum_{n=1}^{N} \exp\left[-(n-1)s\right] \frac{C}{\sqrt{t_n}} \exp\left(-\frac{\tau_1}{t_n} - \frac{t_n}{\tau_2}\right);$$
$$C \sim \frac{Q_0}{\sqrt{\pi D}}; \tau_1 = \frac{z^2}{4D}; \tau_2 = \frac{1}{\lambda}$$

 τ_1 = diffusion time constant τ_2 = decay time constant (both: if larger, then process slower)

Experiments: (by J. Blaauw)

- Periflux 4000 laser Doppler system (Perimed),
- <u>Periflux tissue heater</u> set to 31°C (PF4005, Peritemp),
- Perfusion probe: Laser beam (wavelength 780 nm),
- I<u>ontophoresis probe</u> (PF481-2, Perimed, Sweden) containing a thermostatic probeholder,
- Iontophoresis controller (PeriIont 382, Perimed),
- Position: dorsal side of middle phalanx of third finger,
- <u>Subjects</u> sitting, forearms on soft pillow at heart level,
- <u>Temperature-controlled room</u> (T= $23.4 \pm 0.5^{\circ}$ C)

Laser-Doppler perfusion monitor:

measures 0th and 1st moment of power spectrum of Doppler signal

$$M_n = \int_{\omega_1}^{\omega_2} \omega^n . S(\omega) . d\omega \quad ; \quad n = 0,1$$

 $M_0 \sim \text{concentration of moving (red) blood cells}$ $M_1 \sim \text{perfusion flux (flow)}$ $M_1 / M_0 \sim \text{averaged velocity of blood cells}$

Practical limits: $\omega_1 = 20 \text{ Hz}$; $\omega_2 = 12 \text{ kHz}$

Experiments:

Administered drugs:

- 1. ACh: acetylcholine
- 2. SNP: sodium nitroprusside

Expected: SNP has dilatation effect on vessels and capillaries; this will lead to a higher perfusion.

Subjects for experiments, using in testing the model:

	code	ACh	SNP
Subjects: - Pre-eclampsia patients (Post partum) - Controls (healthy) (Post partum)	PPP PPC	N=22 18	N=21 20
 Experimental settings: Resting flow measurement, duration (s) (¹) Shot duration (s) Current (mA), anodal (A) or cathodal (C) Nr. of shots Shot interval (s) 		600 20 0.1 A 7 60	600 20 0.2 C 9 90

(1): in some cases 100 or 200 s

See LASDOP program

Fit results (2 Pre-eclampsia patients; SNP-administration): 9 shots; 90 sec. apart.



Parameters: $\chi_{2red} = 1.15$; $\tau I = 76 \pm 10$ s; $\tau 2 = 408 \pm 30$ s; $s = 0.029 \pm 0.014$ $\chi_{2red} = 1.90$; $\tau I = 65 \pm 12$ s; $\tau 2 = 252 \pm 30$ s; $s = 0.048 \pm 0.028$ 54



<u>Group:</u> Pre-eclampsia patients; Post-partum; SNP-administration

 $\frac{\text{Time constants:}}{\tau_1 : \text{ diffusion}} \\ \tau_2 : \text{ decay}$

Shot saturation constant: *s* s = 0: all shots contribute; $s \rightarrow \infty$: first shot only

 $\frac{\text{Reduced } \chi^2 :}{= 1 \text{ for optimum fit.}}$

Overall results for post-partum patients (PPP) and post-partum controls (PPC)

4 groups: PPC-ACh, PPC-SNP, PPP-ACh, PPP-SNP

Excluded subjects from calculations, due to off-limit values ($s \ge 10^6$ or $\tau_2 \ge 10^5$ s): 6 of 80; max. 3 of 22.

 $\tau_2 \rightarrow \infty$: decay negligible

s = 0: all shots contribute equally $s \rightarrow \infty$: first shot contributes only

Overall results for post-partum patients (PPP) and controls (PPC)



Conclusions:

PPP = post-partum patients PPC = post-partum controls

- $\tau_1 \sim 1/D$: sign. higher in PPP's (ACh and SNP); slower diffusion
- $\tau_2 \sim T_{1/2}$: sign. higher in ACh's (PPP and PPC); slower **decay**
- s : shot saturation constant: sign. higher in ACh's (PPC and PPP); first shot(s) dominate(s)
- t_M : sign. higher in SNP's (PPC and PPP); see τ_2
- max / resting flux : sign lower in PPC-ACh.
- diffusion coefficients (with $z = 1 \text{ mm resp. 10 } \mu\text{m}$): $\approx 10^4 \text{ resp. 1 x not-electrically sustained values.}$



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