

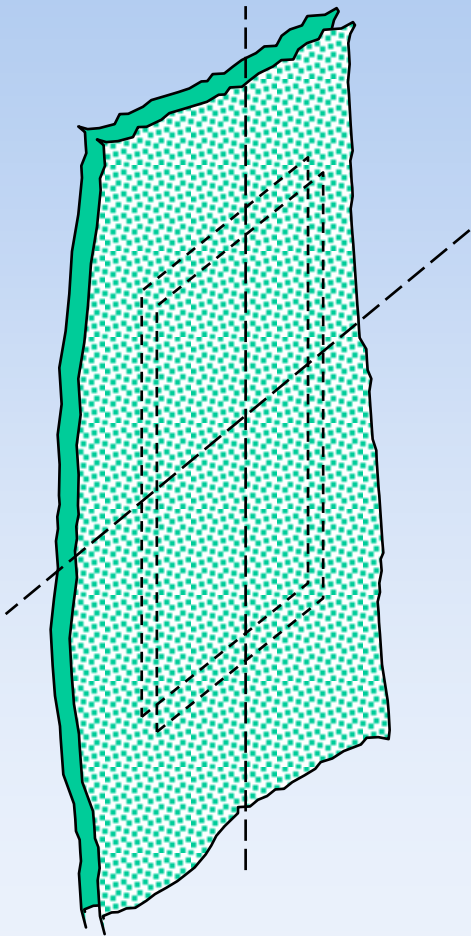
Gauss' Law for Planar Symmetry

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Presentations:

- Electromagnetism: History
- Electromagnetism: Electr. topics
- Electromagnetism: Magn. topics
- Electromagnetism: Waves topics
- Capacitor filling (complete)
- Capacitor filling (partial)
- Divergence Theorem
- E-field of a thin long charged wire
- E-field of a charged disk
- E-field of a dipole
- E-field of a line of dipoles
- E-field of a charged sphere
- E-field of a polarized object
- E-field: field energy
- Electromagnetism: integrations
- Electromagnetism: integration elements
- Gauss' Law for a cylindrical charge
- Gauss' Law for a charged plane
- Laplace's and Poisson's Law
- B-field of a thin long wire carrying a current
- B-field of a conducting charged sphere
- B-field of a homogeneously charged sphere

Gauss' Law for Planar Symmetry



Available:

Thin flat plane, infinitely large,
covered with homogenous
surface charge density σ [C/m²]

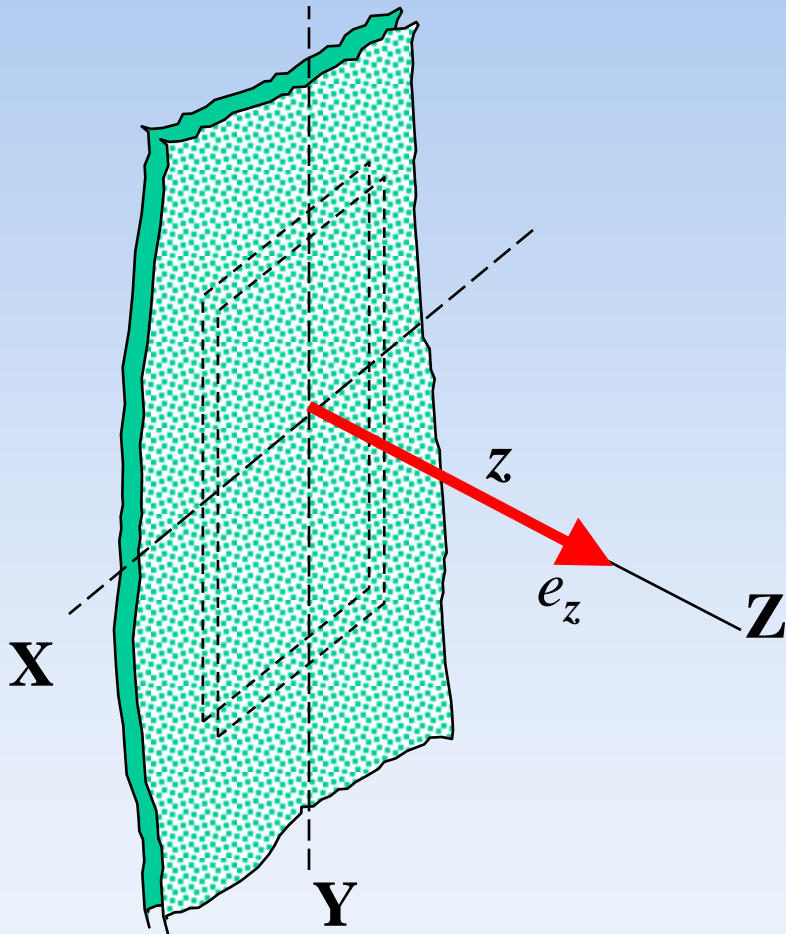
Question:

Calculate E -field at arbitrary
points at both sides of the plane

Gauss' Law for Planar Symmetry

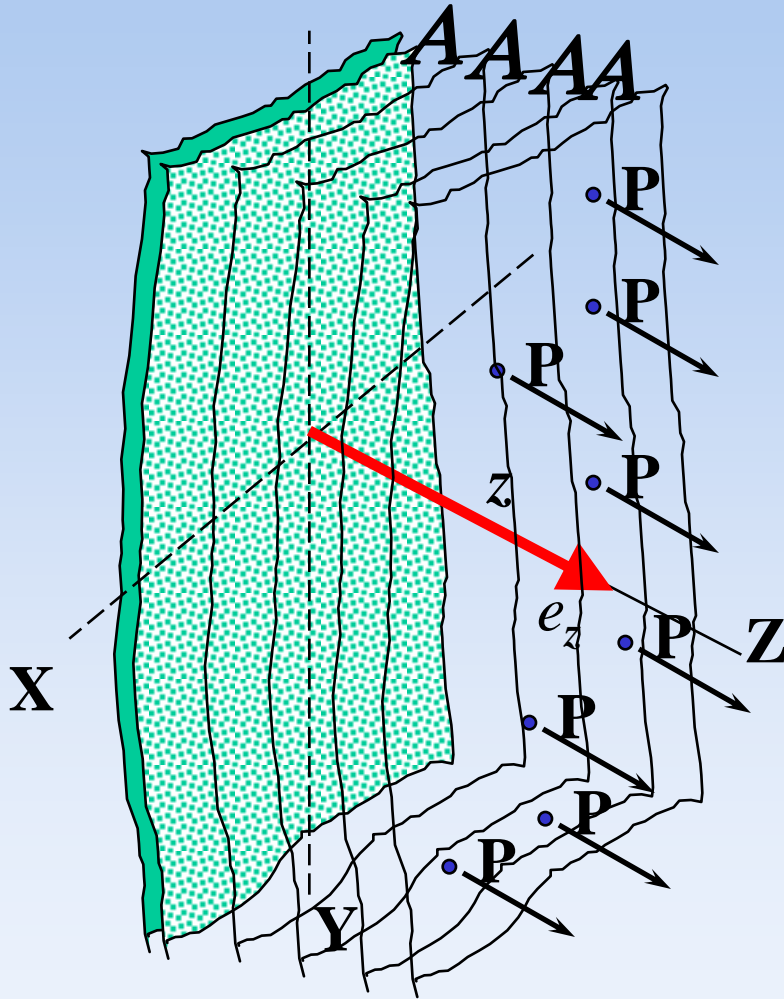
- Analysis and symmetry
- Approach to solution
- Calculations
- Conclusions

Analysis and Symmetry (1)



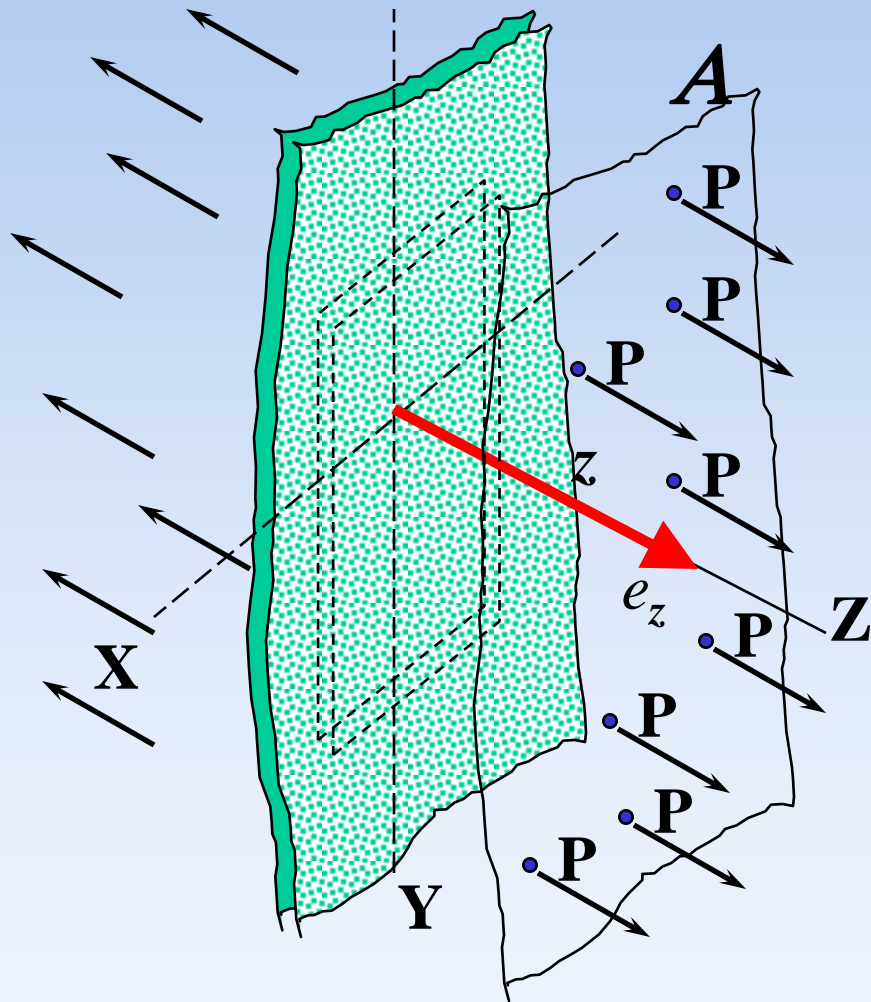
1. Charge distribution:
 σ [C/m²] ; homogeneous.
2. Symmetry:
Z-axis = symm. axis,
perpendicular to plane.
3. Plane: infinitely large.
4. Front & backside are
equivalent.

Analysis and Symmetry (2)



5. Charge distribution:
 σ [C/m²] ; homogeneous.
6. Plane A // charged plane:
7. All points P equivalent
8. Point charge in A:
will not move // A
due to symmetry
9. E : Z-component only !!
10. E : uniform field
11. All A-planes equivalent

Analysis and Symmetry (3)



12. Backside:

similar situation

13. Conclusion from

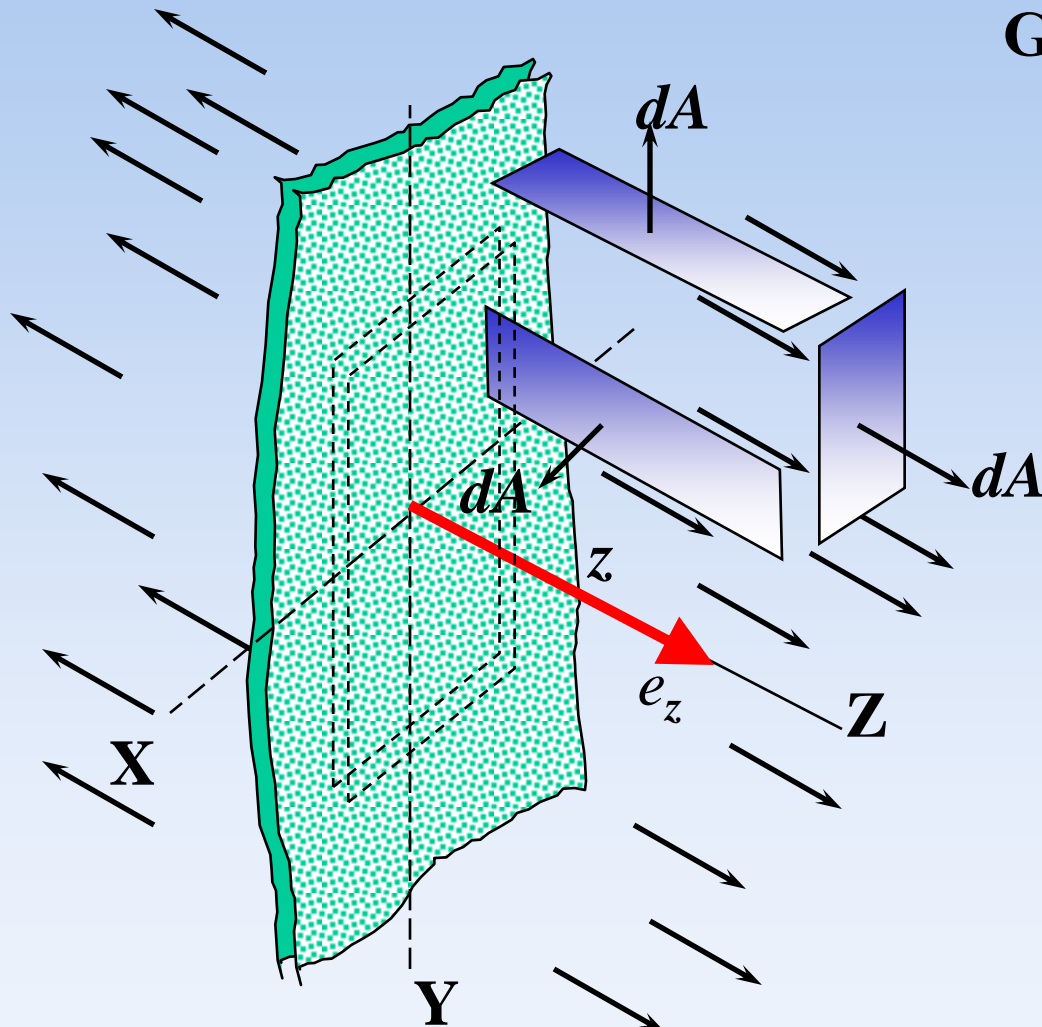
symmetry:

uniform fields;

opposite directions

Gauss' Box (1)

Gauss' Law:
$$\iint_A \mathbf{E} \cdot d\mathbf{A} = \frac{Q}{\epsilon_0}$$

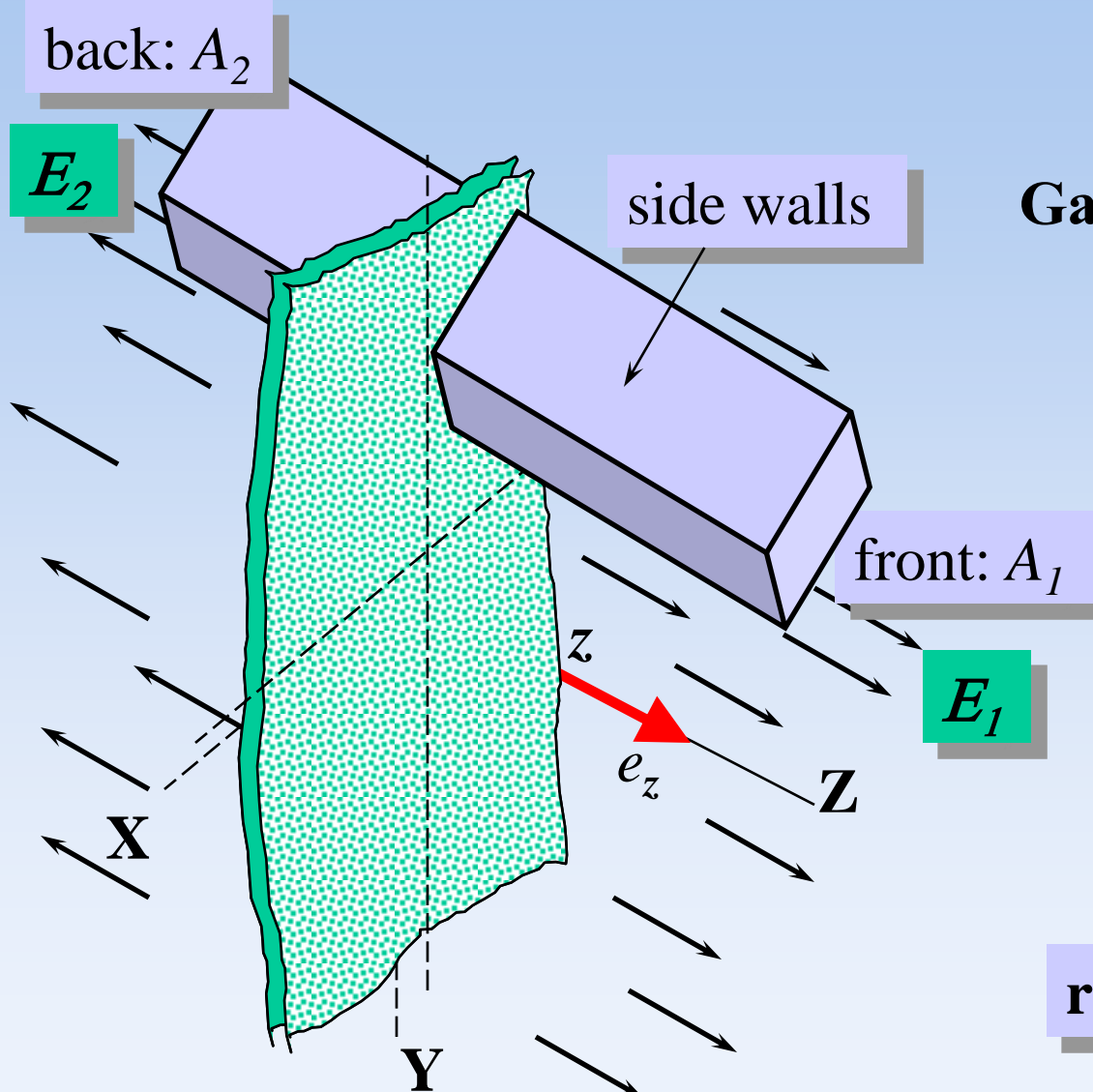


Choose Gauss-box A .
How to make optimum use of symmetry ??

- where $\mathbf{E} \parallel d\mathbf{A}$
- where $\mathbf{E} \perp d\mathbf{A}$
- where $E = 0$??

closed box needed !!
closure at backside
necessary !!

Gauss' Box (2)



Gauss' Law:
$$\iint_A \mathbf{E} \cdot d\mathbf{A} = \frac{Q}{\epsilon_0}$$

choose Gauss-box:

sides do not contribute.

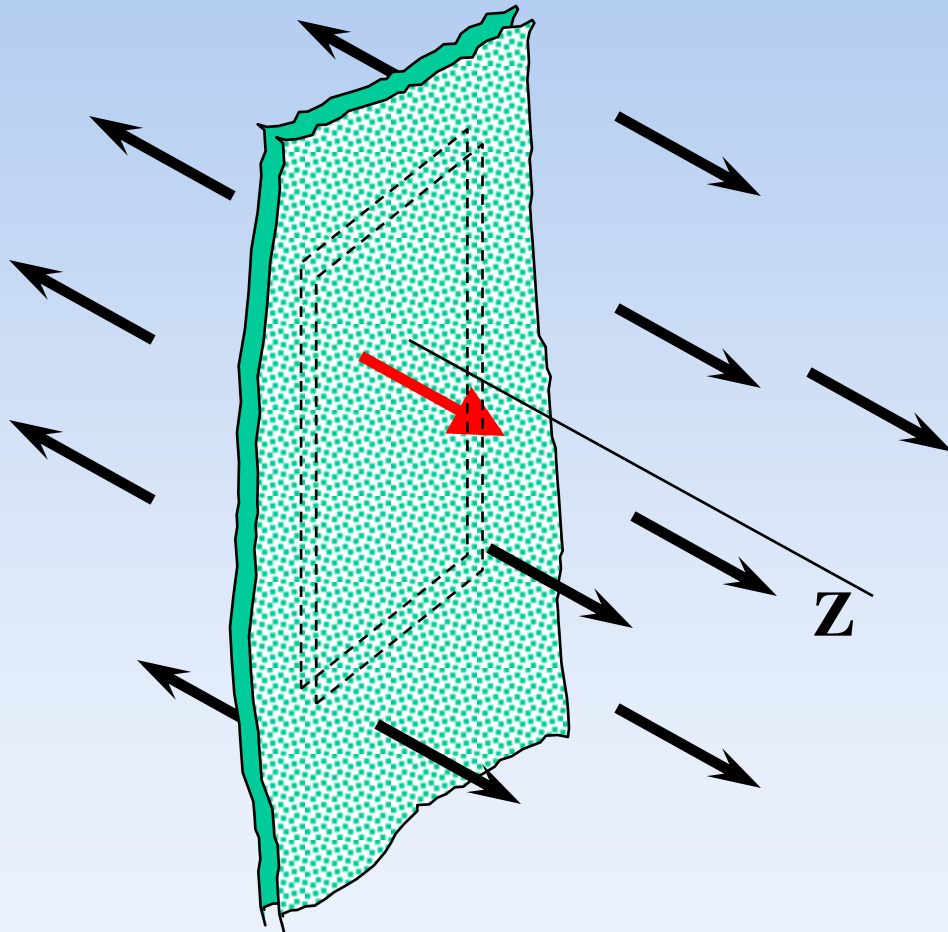
only front and back
lids contribute :

$$E_1 A_1 + E_2 A_2 \quad (A_1 = A_2)$$

charge enclosed: σA_1

result:
$$E_1 = E_2 = \sigma / (2\epsilon_0)$$

Conclusions



for infinite plane:

$$\mathbf{E}_P = \frac{\sigma}{2\epsilon_0} \mathbf{e}_z$$

field strength
independent of
distance to plane =>
homogeneous field

the end